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Economic Dynamics and General Equilibrium

Time and Uncertainty

With 49 Figures
and 26 Tables



Springer

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