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Numerical Linear Algebra

A Concise Introduction
with MATLAB and Julia

Translated by Walter Simson

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